

,

---

,

. . .

---

---

,

"

"

.

8 09.03.04 .

**2004**

681.5.015.32

2004/2005 .

• •

.

• •

, -  
-

1 02.09.2004 .

1

1

:

2

3

2

2.1

$$k_{+1} = k + 2^k, \quad k = 0, 1, 2, \dots,$$

$k^-$

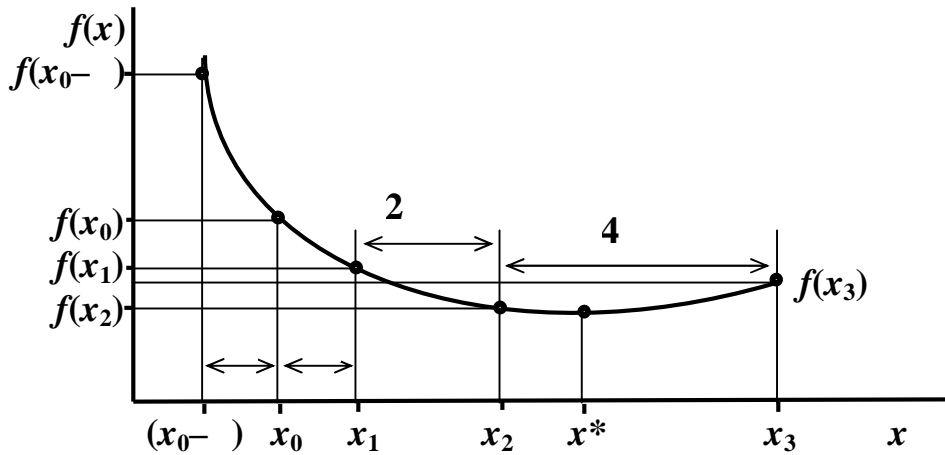
$$f(x_0^-), f(x_0^+) \mid f(x_0^-).$$

$$f(x_0^-) \mid f(x_0) \mid f(x_0^+),$$

(.1).

$$f(x_0^-) \mid f(x_0) \mid f(x_0^+),$$

$$(x_0^-) \mid (x_0^+)$$



1 -

$$f(x) = f(0) + f'(0)x + \frac{f''(0)}{2!}x^2 + \dots$$

## 2.2

### 2.2.1

$f(x)$

$f(x)$

$f(x)$

$a$   $b$ ,

$$a < x_1 < x_2 < b.$$

$x_1$   $x_2$ ,

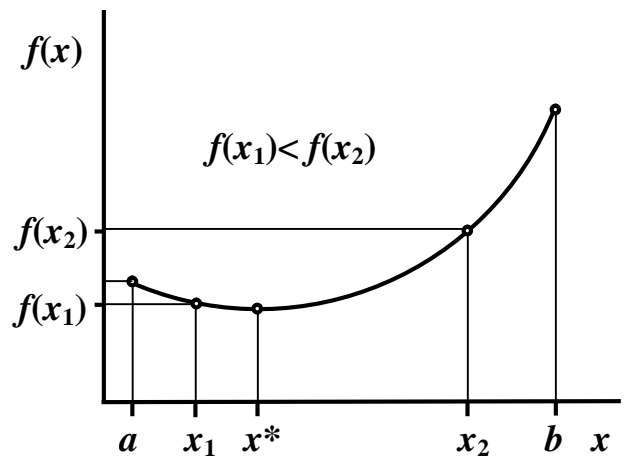
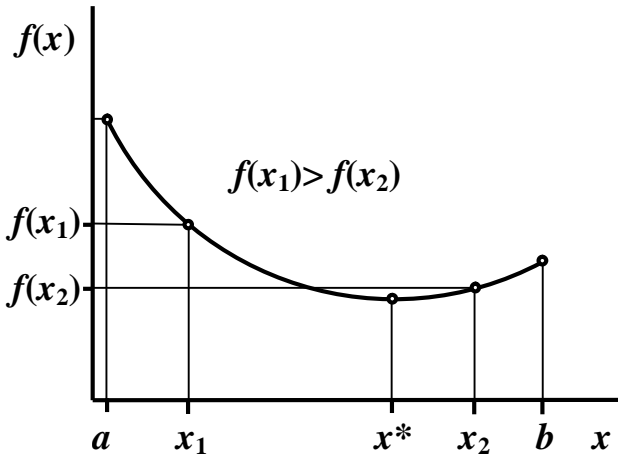
$x_1$   $x_2$ ,

1.  $f(x_1) > f(x_2)$ ,  
 $x^* \in (x_1, x_2)$ .

$f(x)$   $(x_1, x_2)$ ,

2.  $f(x_1) < f(x_2)$ ,  
 $x^* \in (x_1, x_2)$ .

$f(x)$   $(x_2, x_1)$ ,

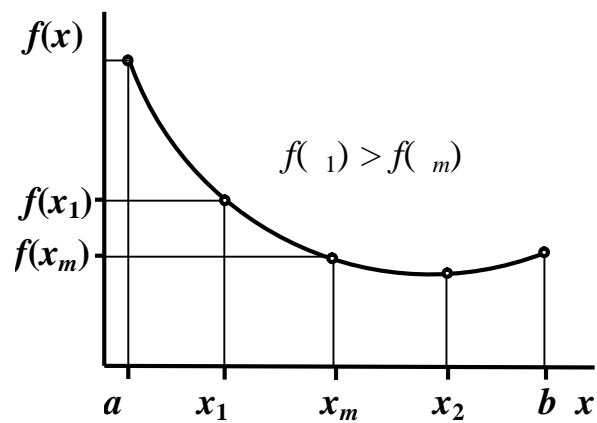
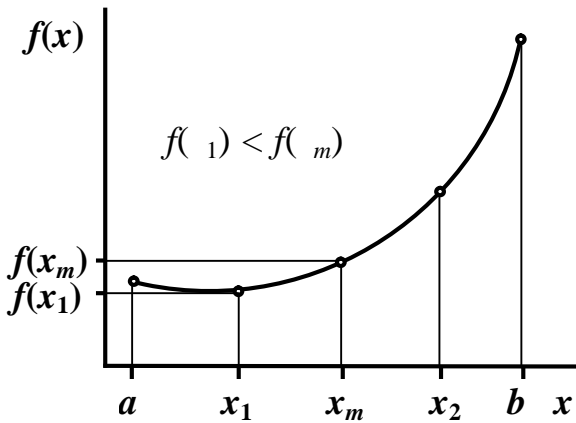


)  
2-

$f(x_1) = f(x_2)$ ,  
 $(x_1, f(x_1))$   $(x_2, f(x_2))$ ,  
 $(x_1, x_2)$ .

2.2.2

$f(x)$   $(a, b)$ ,



)  
3-

1.  $x_m = (a + b) / 2$   $L = b - a$   $f(x_m)$ .
2.  $x_1 = a + L/4$   $x_2 = b - L/4$   $(x_1, f(x_1))$   $(x_2, f(x_2))$   $(x_1, x_2)$   $f(x_1)$   $f(x_2)$ .

$f(x_2)$ .

3.  $f(x_1) < f(x_m)$ .

(1)  $f(x_1) < f(x_m)$  ( . 3, ),  $(m, b)$ ,  
 $b = m$ . 1. , -

$x_m = 1$ . 5.  
 (2)  $f(x_1) < f(x_m)$  ( . 3, ), 4.  
 4.  $f(x_2) < f(x_m)$ .

(1)  $f(x_2) < f(x_m)$ ,  $(, m)$ ,  $= m$ .  
 2  $m = 2$ .

5.

(2)  $f(x_2) < f(x_m)$ ,  $(, 1)$   $(2, b)$ .  $a = 1$   
 $b = 2$ . ,  $m$  -

5.  $L = b -$  . 5.  $|L|$  , .  
 2.

1.

2.

1, 2  $m$ , . ,  
 ;

3.

$(1/2)^{n/2}$

4.

[3]

( , , . ) , -  
 , .

**2.2.3**

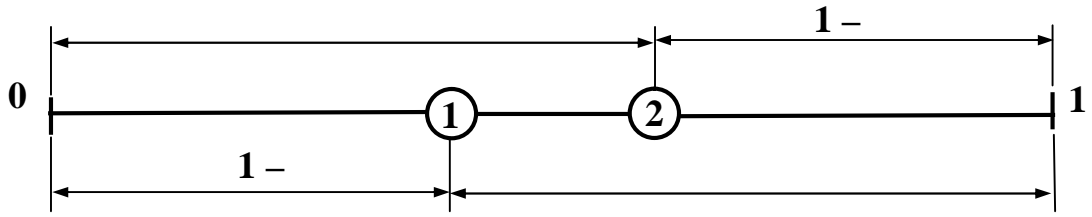
1.

2.

3.

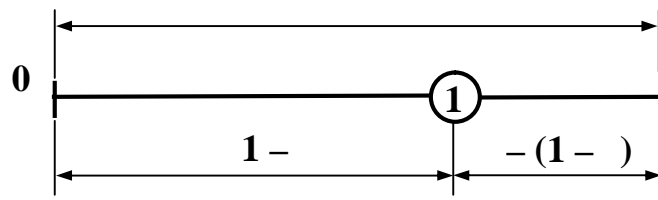
. 4. ( . )

, , -  
 , -



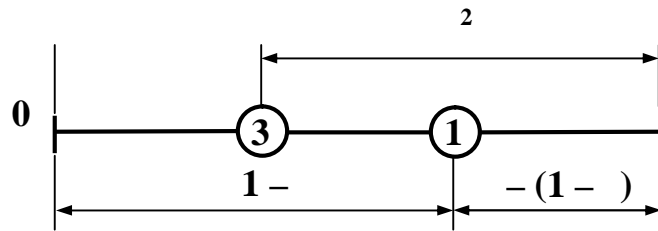
4-

, .5 ,  
(1 - ) .



5-

, (1 - ) -  
( , ).  
, -  
( .6).



6-

, ( .4) 1 -  
, / 1 = (1 - ) / . : 1 - = ^2.

$$= (-1 \pm \sqrt{5})/2,$$

$$= 0,61803... .$$

, ( .4)  
, (1, 2) - (1 - ):

$$\frac{-(1-)}{1-} = \frac{1-}{1-},$$

$$^2 - (1 - ) = (1 - )^2.$$

$$(1 - ).$$

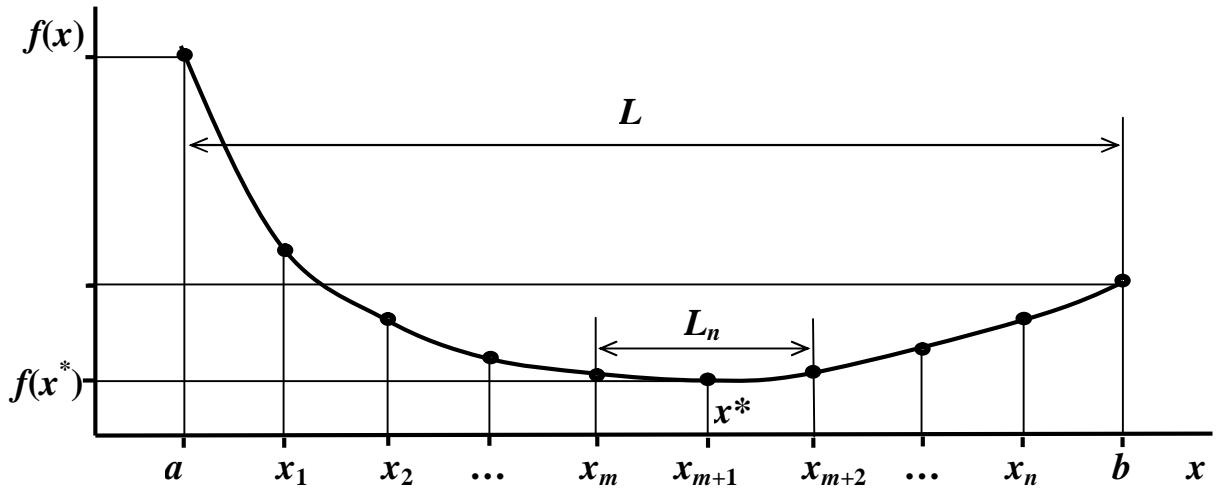
$2 = 1 - \dots$   
 $1 - = 2$   
 $.4,$   
 $.6.$   
 $(1 - )-$   
 $n$   
 $n-1$   
 $(XR XL)$   
 $w = XR - n \quad w = XL - n,$   
 $n$   
 $(, ,$   
 $),$

**2.2.4**

$L,$   
 $L_n.$   
 $K_L(n) = L_n / L.$   
 $L(0,618)^{n-1},$   
 $L(0,5)^{n/2}$   
 $K_L(n) = 0,5^{n/2} -$   
 $K_L(n) = 0,618^{n-1} -$   
 $(.7),$   
 $L$   
 $(n + 1)$



$L/(n + 1)$ ,  $*$  - ,  $f(x)$ .  
 $\{ [ * - L/(n + 1)], [ * + L/(n + 1)] \}$ ,  
 $L_n = 2L/(n+1)$ .



7 -

. 2.1  $K_L(n) = 2/(n+1)$ .  
 $K_L(n)$ ,  $n$ ,

2.1 -

	$n = 2$	$n = 5$	$n = 10$	$n = 15$	$n = 20$
	0,5	0,177	0,031	0,006	0,0009
	0,618	0,146	0,013	0,001	0,0001
	0,667	0,333	0,182	0,125	0,095

$K_L(n) =$  ,  
 $n$  :  
 $n = 2 \ln( ) / \ln(0,5)$ ;  
 $n = l + [\ln(E) / \ln(0,618)]$ ;  
 $n = (2/E) - 1$ .

. 2.2

, -  
.

2.2 –

	= 0,1	= 0,05	= 0,01	= 0,001
		7	9	14
	5	8	11	16
	19	36	199	1999

, -  
, -  
.**3**

3.1

3.2

,

3.3

?

3.4

3.5

3.6

3.7

?

3.8

.

**4**

4.1

«

».

4.2

,

4.3

**5**

5.1

,

5.2

1, 2 3

.

$$1. \quad f(x) = (100 - x)^2$$

$x_0 = 30 \quad | \quad \Delta x = 5.$

$$f(x_0) = f(30) = 4900,$$

$$f(x_0 + \Delta x) = f(35) = 4225,$$

$$f(x_0 - \Delta x) = f(25) = 5625.$$

$$f(x_0 - \Delta x) > f(x_0) > f(x_0 + \Delta x),$$

30.

$$x_1 = x_0 + \Delta x = 35. \quad x_2 = x_1 + \Delta x = 45,$$

$$f(45) = 3025 < f(x_1),$$

\* &gt; 35.

$$x_3 = x_2 + \Delta x^2 = 65, \quad f(65) = 1225 < f(x_2),$$

\* &gt; 45.

$$x_4 = x_3 + \Delta x^3 = 105, \quad f(105) = 25 < f(x_3),$$

\* &gt; 65.

$$x_5 = x_4 + \Delta x^4 = 185, \quad f(185) = 7225 > f(x_4),$$

, \* &lt; 185.

$$65 \quad * \quad 185,$$

\*.

$$2. \quad f(x) = (100 - x)^2 \quad 60 \quad 150. \quad = 60, b = 150$$

$$L = 150 - 60 = 90.$$

$$m = (60 + 150)/2 = 105.$$

1

$$x_1 = a + (L/4) = 60 + (90/4) = 82,5,$$

$$x_2 = b - (L/4) = 150 - (90/4) = 127,5,$$

$$f(82,5) = 306,25 > f(105) = 25,$$

$$f(127,5) = 756,25 > f(105).$$

,

$$(60, 82,5) \quad (127,5, 150).$$

$$90 \quad 45.$$

2

$$a = 82,5, b = 127,5, \quad m = 105,$$

$$L = 127,5 - 82,5 = 45,$$

$$x_1 = 82,5 + (45/4) = 93,75,$$

$$x_2 = 127,5 - (45/4) = 116,25,$$

$$f(93,75) = 39,06 > f(105) = 25,$$

$$f(116,25) = 264,06 > f(105).$$

,

$$(93,75, 116,25).$$

$$\begin{aligned}
 &= 93,75, \quad b = 116,25, \quad m = 105, \\
 L &= 116,25 - 93,75 = 22,5, \\
 a_1 &= 99,375, \quad a_2 = 110,625, \\
 f(a_1) &= 0,39 < f(105) = 25.
 \end{aligned}$$

$$\begin{aligned}
 & \quad , \quad (105, 116,25). \\
 & \quad (93,75, 105), \quad 99,375 \left( \frac{1}{2} \right) \\
 3). \quad & \quad , \quad ( \\
 & \quad 90 \quad 90 \times (1/2)^3 = 11,25.
 \end{aligned}$$

$$\begin{aligned}
 & \quad 3. ( \quad ) \\
 f(x) &= (100 - x)^2 \quad 60 < x < 150. \\
 & \quad 1,
 \end{aligned}$$

$$\begin{aligned}
 & \quad , \quad w = (x - 60)/90, \\
 & \quad f(w) = (40 - 90w)^2 \\
 & \quad 0 \leq w \leq 1. \\
 1. \quad & I_1 = (0, 1); L_1 = 1.
 \end{aligned}$$

$$\begin{aligned}
 & \quad : \\
 w_1 &= 0,618, \quad f(w_1) = 244,0, \\
 w_2 &= 1 - 0,618 = 0,382, \quad f(w_2) = 31,6. \\
 & \quad f(w_2) < f(w_1) \quad w_2 < w_1, \quad w = w_1. \\
 2. \quad & I_2 = (0, 0,618); L_2 = 0,618 = .
 \end{aligned}$$

$$\begin{aligned}
 w_3 &= 1 - 0,382 = (1 - 0,382) = 0,618, \quad f(w_3) = 352. \\
 & \quad f(w_3) > f(w_2) \quad w_3 < w_2, \quad w = w_3. \\
 3. \quad & I_3 = (0,236, 0,618), L_3 = 0,382 = . \\
 & \quad , \quad \times (
 \end{aligned}$$

$$\begin{aligned}
 (1 - 0,236) &\times ( \\
 w_4 &= 0,618 - (1 - 0,236) L_3 = 0,618 - 0,236 L_3 = 0,618 - 0,236 \times 0,382 = 0,618 - 0,09 = 0,472, \\
 f(w_4) &= 6,15. \\
 & \quad f(w_4) > f(w_2) \quad w_4 < w_2, \quad w = w_2.
 \end{aligned}$$

$$\begin{aligned}
 0,382 \quad w \quad 0,618 \quad w, \quad 94,4 \quad w \quad 115,6
 \end{aligned}$$

$$\begin{aligned}
 & \quad w \\
 N-1 = 5 &= 0,09, \\
 & \quad 8,1
 \end{aligned}$$

$$11,25.$$

1.

$$f(x) = (N0 - 2x)^2$$

$$f(0) = \frac{N0}{M} = \frac{N0}{3M}$$

$N -$  ; -

$N = 15.$  , -

$= 5.$  , -

$= 4.$  , -

2.

$f(x) = (N0 - 2x)^2$   $\frac{N0}{M}$   $K(N0).$

$N -$  ; -

$N = 15.$  , -

$= 2, = 5.$  , -

$= 3, = 4.$  , -

3.

$f(x) = (N0 - 2x)^2$   $f(x)$

$N -$  ; -

$N = 15.$  , -

$= 2, = 5.$  , -

$= 3, = 4.$  , -

**6**

1 .

2 ,

3 .

4 .

5 -

## 7

1 . . . , . . .  
: . / . . . . - , 1988. - .1. - 86 .  
2 . . . . : 2- .  
. 1 - . : , 1986. - 352 .  
3 . . . . - . . .  
. , 1973.



